

MOHID Whish list

Numerics

- Faster: Lagrangian and Eulerian => parallelisation
- Data Assimilation

2-Way Nesting

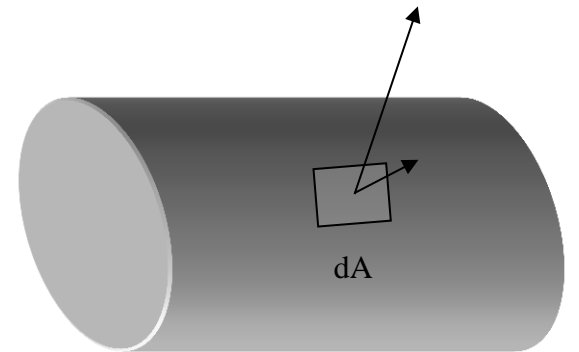
- Increases speed and Assimilation learning

Assimilation/Nudging/Relaxation

- Assimilation is the act of modifying a solution using external data. The scarcer is data, the most difficult assimilation is.
- Assimilation of gridded data is easy and gets different names

Advection – Diffusion Equation and Code Structure

*{The rate of accumulation of a property inside a control volume} =
{what flows in minus what flows out} + {Production minus Consumption}*



$$\frac{\partial}{\partial t} \left(\iiint_{Vol} \beta dVol \right) = - \iint_A \beta (\vec{v} \cdot \vec{n}) dA - \iint_A -\vartheta (\vec{\nabla} \beta \cdot \vec{n}) dA + Sources - Sinks$$

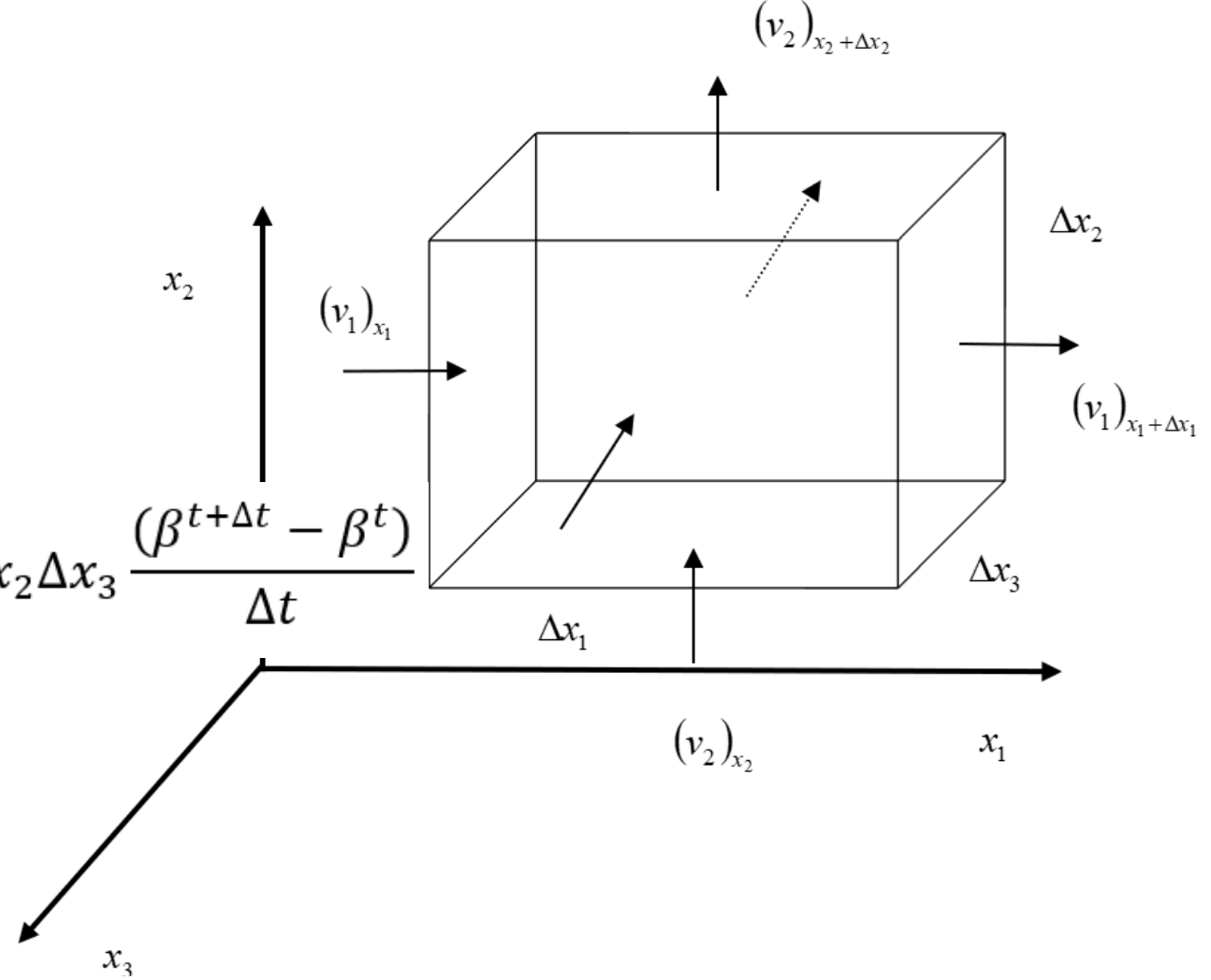
- This equation was easy to obtain, it is easy to understand, but it is not useful to get results because the integrals very seldom have a solution.

Algebraic Equation

$$Vol = \Delta x_1 \Delta x_2 \Delta x_3 \quad \blacktriangleright \text{Constant in time}$$

$$A_k = \Delta x_i \Delta x_j$$

$$\frac{\partial B}{\partial t} = \frac{\partial}{\partial t} \left(\iiint_{Vol} \beta dVol \right) = \frac{B^{t+\Delta t} - B^t}{\Delta t} = \Delta x_1 \Delta x_2 \Delta x_3 \frac{(\beta^{t+\Delta t} - \beta^t)}{\Delta t}$$



$$\begin{aligned} \Phi_{adv} = - \iint_A \beta (\vec{v} \cdot \vec{n}) dA = & \Delta x_2 \Delta x_3 [(\beta v_1)_{x_1} - (\beta v_1)_{x_1 + \Delta x_1}] \\ & + \Delta x_1 \Delta x_3 [(\beta v_2)_{x_2} - (\beta v_2)_{x_2 + \Delta x_2}] \\ & + \Delta x_1 \Delta x_2 [(\beta v_3)_{x_3} - (\beta v_3)_{x_3 + \Delta x_3}] \end{aligned}$$

Differential Equation

$$\frac{\partial \beta}{\partial t} + \frac{\partial \beta v_i}{\partial x_i} = \vartheta \frac{\partial^2 \beta}{\partial x_i^2} + \text{sources} - \text{sinks}$$

➤ Or,

$$\frac{\partial \beta}{\partial t} = -\frac{\partial}{\partial x_i} \left(\beta v_i - \vartheta \frac{\partial \beta}{\partial x_i} \right) + \text{sources} - \text{sinks}$$

➤ If incompressible flow the divergence of the velocity is zero and the equation becomes:

$$\frac{\partial \beta}{\partial t} + v_i \frac{\partial \beta}{\partial x_i} = \vartheta \frac{\partial^2 \beta}{\partial x_i^2} + \text{sources} - \text{sinks}$$

➤ If the control volume was moving at the flow velocity, the relative velocity would be zero and there would be no advection => Lagrangian formulation

➤ Source/Sink code must be share by both formulations!!!

Source/Sinks



Who took this decision?

In the code, predation is done in the predator subroutine/module and not in the prey subroutine/module!!!

What happens to the prey?

- It is respired!
- What is that?
- $\text{CO}_2 + \text{H}_2\text{O} + \text{PO}_4 + \dots + \text{Detritus}$
- What happens to the detritus?
-

How to implement this?

Subroutines/Modules should describe activities of specific functional groups. NH4 has no activity and thus should have no subroutine!

Fractionated Time-Step is **A** numerical support for that. It is better than the explicit algorithm (stability and accuracy)

$$\frac{\partial P}{\partial t} = \frac{P^{t+\Delta t} - P^t}{\Delta t} = \frac{P^{t+\Delta t} - P^*}{\Delta t} + \frac{P^* - P^{**}}{\Delta t} + \frac{P^{**} - P^t}{\Delta t}$$

In MOHID we also have an implicit algorithm